

## Structure and Thermal Expansion of $\text{LiGe}_2(\text{PO}_4)_3$

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$\text{LiGe}_2(\text{PO}_4)_3$  belongs to the Nasicon-type family. Room-temperature structure has been determined on a single crystal from 3D X-ray data. Thermal evolution of this structure has been established from neutron powder diffraction data between 300 and 1000 K using the Rietveld method. The thermal expansion is positive along the *c*-axis, whereas shrinking is observed along the *a*-axis below 900 K, followed by dilatation. The atomic displacements noted with increasing temperature are consistent with a model proposed for  $\text{NaZr}_2(\text{PO}_4)_3$ . © 1991 Academic Press, Inc.

The  $\text{LiGe}_2(\text{PO}_4)_3$  phosphate may occur both in crystalline state and in vitreous state (1). The crystallized species has Nasicon-type structure. Several members of this structural family are near zero thermal expansion materials and have industrial applications (2-4). The existence of a glass of similar composition opened the possibility of elaborating a low-thermal expansion glass-ceramic.

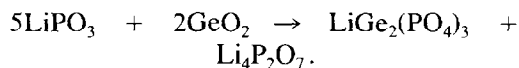
In this general scope the present investigation covers:

- (i) crystal structure determination of  $\text{LiGe}_2(\text{PO}_4)_3$  from X-ray single crystal data, and
- (ii) thermal expansion investigation of the

ceramic by neutron diffraction structure analysis between room temperature and 1000 K.

### Crystal Structure of $\text{LiGe}_2(\text{PO}_4)_3$ at Room Temperature from X-Ray Diffraction

Single crystals of  $\text{LiGe}_2(\text{PO}_4)_3$  were obtained by a flux technique; the germanium oxide is dissolved in an excess of  $\text{LiPO}_3$  with respect to following reaction:



The mixture was heated in air for several hours at 1050°C and then cooled at a rate of

TABLE I  
CONDITIONS USED FOR DATA COLLECTION OF  $\text{LiGe}_2(\text{PO}_4)_3$  SINGLE CRYSTAL

Radiation	MoK $\alpha$ (graphite monochromatized) $\lambda = 0.7107 \text{ \AA}$
$T = 20^\circ\text{C}$	
Scanning	$\omega$
Angular range	$0.1 < \theta < 35^\circ$
$hkl$ limits of the explored reciprocal space	$-13 \leq h \leq 12$ $-13 \leq k \leq 13$ $-13 \leq l \leq 32$
Scanning width counter slit width	$0.86 + 0.44 \tan \theta$ ( $^\circ$ ) $0.09 + 0.21 \tan \theta$ (mm)
Total number of measured reflections	3.472
Independent data $F_o^2 > 3 \sigma (F_o^2)$ : 527	
	$R_{\text{INT}} = \frac{\sum \sum [F_o - \langle F_o \rangle]}{\sum F_o} = 0.031$

Note. The data were corrected for Lorentz-polarization effects but not for absorption ( $\mu_R = 0.8$ ).

$5^\circ\text{C hr}^{-1}$  down to  $400^\circ\text{C}$ . Single crystals were extracted by removing the lithium diphosphate with hot water.

The crystallographic investigation was carried out on a crystal of parallelepipedic shape ( $120 \times 190 \times 220 \mu\text{m}$ ). The Laue photographs gave evidence of a trigonal symmetry. Systematic absences

$$\begin{aligned} (hkl): -h + k + l &\neq 3n \\ (hhl): h + l &\neq 3n; \quad l \neq 2n \end{aligned}$$

are compatible with the  $R\bar{3}c$  or  $R3c$  space group.

The cell parameters were refined using 22 reflections from X-ray powder diffraction (the internal standard was Al), either

$$\begin{aligned} a_{\text{H}} &= 8.275(5) \text{ \AA}; \quad c_{\text{H}} = 20.47(3) \text{ \AA}, \\ \text{or } a_{\text{R}} &= 8.33 \text{ \AA}; \quad \alpha_{\text{R}} = 59.6^\circ. \end{aligned}$$

The measured specific mass ( $3.56 \text{ g cm}^{-3}$ ) is in good agreement with the calculated one ( $3.61 \text{ g cm}^{-3}$  with  $Z = 6$  in the hexagonal cell).

Data collection was achieved with an ENRAF-NONIUS CAD3 automatic dif-

fractometer and with conditions given in Table I.

All calculations were made with the SHELX 76 (5) program in the  $R3c$  space group. Atomic scattering factors and anomalous dispersion corrections were taken from "International Tables for X-Ray Crystallography" (6).

All nonlithium atoms were located using the  $\text{NaZr}_2(\text{PO}_4)_3$  structure as a model (7). In those conditions, assuming individual isotropic thermal parameters for all atoms, the  $R$  factor was 0.12. A difference Fourier synthesis revealed a residual peak at the origin, i.e., at the  $M_1$  site (6b). There is no significant electron density near the second possible site, i.e.,  $M_2$  (18e) (20).

Calculations were carried out assuming the lithium ions to be distributed over both  $M_1$  and  $M_2$  sites with a refinement of the correlated occupation factors. They confirm only occupancy of the  $M_1$  site.

A final calculation was achieved with lithium ions at the origin (site  $M_1$ ), but now using individual anisotropic thermal parameters for all atoms, a weighting factor  $w = 1/\sigma^2 (F_o)$  and an empirical isotropic extinc-

TABLE II  
ATOMIC PARAMETERS OF LiGe<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub>

Atoms	Position	Site symmetry	x	y	z	Beq(Å) <sup>2</sup>
Li	6b	$\bar{3}$	0	0	0	2.44
Ge	12c	3.	0	0	0.14097(1)	0.26
P	18e	.2	0.2879(1)	0	$\frac{1}{4}$	0.28
O <sub>1</sub>	36f	1	0.1802(2)	-0.0152(2)	0.1883(1)	0.85
O <sub>2</sub>	36f	1	0.1845(2)	0.1593(2)	0.0821(1)	0.65
$\times 10^4 (\text{\AA})^2$						
	<i>U</i> <sub>11</sub>	<i>U</i> <sub>22</sub>	<i>U</i> <sub>33</sub>	<i>U</i> <sub>23</sub>	<i>U</i> <sub>13</sub>	<i>U</i> <sub>12</sub>
Li	405(50)	<i>U</i> <sub>22</sub>	118(45)	0	0	<i>U</i> <sub>11</sub> /2
Ge	30(1)	<i>U</i> <sub>11</sub>	37(2)	0	0	<i>U</i> <sub>11</sub> /2
P	26(2)	34(3)	49(3)	12(2)	<i>U</i> <sub>23</sub> /2	<i>U</i> <sub>22</sub> /2
O <sub>1</sub>	103(6)	138(7)	106(6)	6(5)	-45(5)	77(5)
O <sub>2</sub>	52(5)	65(6)	81(5)	10(5)	10(4)	-8(5)

Note. Atomic coordinates and equivalent isotropic parameters for LiGe<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> (Beq =  $(8\pi^2/3) \sum_{i=1}^3 \sum_{j=1}^3 a_i^* a_j$  *U*<sub>ij</sub> (**a**<sub>i</sub> · **a**<sub>j</sub>)).

*U*<sub>ij</sub> coefficients of anisotropic thermal parameters.  $T - \exp - 2\pi^2(h^2a^{*2}U_{11} + k^2b^{*2}U_{22} + l^2c^{*2}U_{33} + 2hka^*b^*U_{12} + 2hla^*c^*U_{13} + 2klb^*c^*U_{23})$ .

tion parameter  $x$  ( $F_c = F(1 - 10^{-4} \cdot x \cdot F^2/\sin \theta)$ ). It converged down to  $x = 0.0029(1)$ , with  $R = 0.0239$  and  $R_w = 0.0236$ . The obtained atomic parameters are given in Table II.

TABLE III

INTERATOMIC ANGLES AND DISTANCES IN LiGe<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> (ROOM TEMPERATURE AND X-RAY DIFFRACTION DATA)

Li-O <sub>2</sub> : 6 × 2.210(1) (Å)	O <sub>2</sub> -Li-O <sub>2</sub> i: 68.4(0.1)°
Ge-O <sub>1</sub> : 3 × 1.834(1) (Å)	O <sub>1</sub> -Ge-O <sub>1</sub> i: 94.7(0.1)°
	O <sub>1</sub> -Ge-O <sub>2</sub> : 89.0(0.1)°
Ge-O <sub>2</sub> : 3 × 1.872(1) (Å)	O <sub>1</sub> -Ge-O <sub>2</sub> i: 171.5(0.1)°
	O <sub>1</sub> -Ge-O <sub>2</sub> ii: 92.6(0.1)°
	O <sub>2</sub> -Ge-O <sub>2</sub> i: 83.1(0.1)°
P-O <sub>1</sub> : 2 × 1.515(1) (Å)	O <sub>1</sub> -P-O <sub>1</sub> iv: 113.7(0.1)°
	O <sub>1</sub> -P-O <sub>2</sub> iii: 112.9(0.1)°
P-O <sub>2</sub> iii: 2 × 1.530(1) (Å)	O <sub>1</sub> -P-O <sub>2</sub> v: 104.2(0.1)°
	O <sub>2</sub> iii-P-O <sub>2</sub> v: 109.1 (0.1)°

Note. Symmetry operation codes: i, -y, x - y, z; ii, y - x, -x, z; iii,  $\frac{2}{3} - x, \frac{1}{3} - y, \frac{1}{3} - z$ ; iv, x - y, -y,  $\frac{1}{2} - z$ ; v,  $\frac{1}{3} + y - x, -\frac{1}{3} + y, -\frac{1}{3} + \frac{1}{2} + z$ .

The thermal motion of lithium exhibits a relatively strong anisotropic character with greater displacements in the (a, b) plane than along the c-axis. This anisotropy in the M<sub>1</sub> site is in good agreement with the Nasicon lattice model. The Beq parameter has a reasonable value (2.44 Å<sup>2</sup>). In addition calculations involving a Li<sup>+</sup> ion-delocalization in the plane (a, b) near the origin lead to a nonsignificant weak value of x, strongly correlated with thermal parameters.

The interatomic distances and angles calculated for LiGe<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> from the X-ray diffraction data are given in Table III.

### Crystal Structure of LiGe<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> Determined by Neutron Diffraction Investigation

The powder of LiGe<sub>2</sub>(PO<sub>4</sub>)<sub>3</sub> was prepared as previously described (1).

The neutron diffraction patterns were collected at ILL with the powder diffractometers D<sub>1A</sub> (room temperature) and D<sub>1B</sub> (300–1000 K). The neutron diffraction data

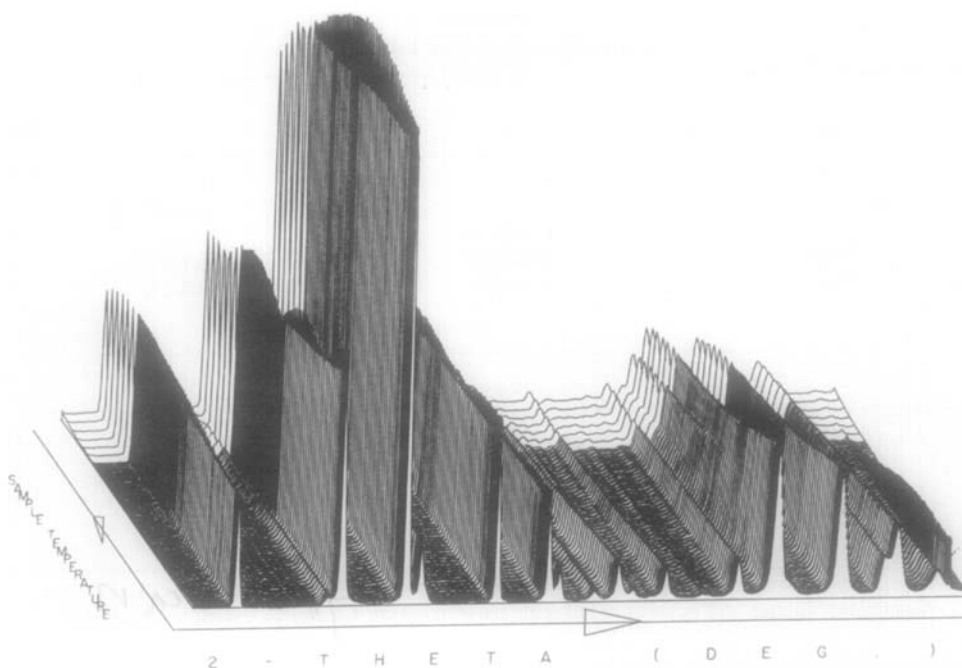


FIG. 1. Neutron diffraction patterns of  $\text{LiGe}_2(\text{PO}_4)_3$  between 300 and 1000 K.

have been analyzed by the Rietveld profile method (8).

As the neutron diffractograms revealed the existence of  $\text{GeO}_2$  as a minor parasitic phase, we utilized a refinement program allowing us to calculate simultaneously the parameters and intensities of both phases.

A tridimensional projection of the thermodiffractograms between 295 and 1000 K is given in Fig. 1.

About 80 structure determinations were carried out within this temperature range. Refinements converged to atomic positions very close to those found by X-ray diffraction except in the description of the  $\text{Li}^+$  site. For lithium located in the (0,0,0) site the isotropic thermal factor is  $B = 2.6 \text{ \AA}^2$ . Lowering  $R$  supposes a lithium shift to an off-centered position in the basal ( $a, b$ ) plane (with a large standard deviation) and a related decrease of  $B$ .

All previously reported results concerning the structure either of  $\text{LiTi}_2(\text{PO}_4)_3$  (9)

or of  $\text{LiZr}_2(\text{PO}_4)_3$  (10) gave evidence of the highly anisotropic character of the thermal parameters associated with the lithium position in the ( $a, b$ ) plane.

Table IV compares the final atomic coordinates obtained at 300 K by both X-ray and neutron diffraction techniques.

In the following discussion we shall assume the lithium ions to have average 0,0,0 coordinates similar to those of  $\text{LiTi}_2(\text{PO}_4)_3$  or  $\text{LiZr}_2(\text{PO}_4)_3$ .

Figure 2 shows the thermal expansion of the crystal lattice of  $\text{LiGe}_2(\text{PO}_4)_3$  between 300 and 1000 K and the corresponding mean thermal expansion coefficients  $\langle \alpha \rangle$ .

At high temperature  $\text{LiGe}_2(\text{PO}_4)_3$  remains trigonal. At rising temperature the  $c$ -parameter increases, whereas the  $a$ -parameter decreases between 300 and 900 K and then increases.

Phosphorus, zirconium, and oxygen keep the same positions in the investigated temperature range. Examples of evolution of

TABLE IV  
ATOMIC PARAMETERS OF  $\text{LiGe}_2(\text{PO}_4)_3$

	Neutrons $\lambda = 1.912 \text{ \AA}$ $N_{hkl} = 140$	Neutrons $\lambda = 2.524 \text{ \AA}$ $N_{hkl} = 32$	X-ray $\lambda = 0.7107 \text{ \AA}$ $N_{hkl} = 527$
$a(\text{\AA})$	8.2722(2)	8.2682(9)	8.272(5)
$c(\text{\AA})$	20.4825(7)	20.494(4)	20.47(3)
Li <sub>1</sub>			
$x$	0.025(2)	0.025	0
$y$	0	0	0
$z$	0	0	0
$B(\text{\AA})^2$	1.3(6)	0.9(3)	2.44
Ge			
$x$	0	0	0
$y$	0	0	0
$z$	0.1412(1)	0.1403(8)	0.14097(1)
$B(\text{\AA})^2$	0.84(7)	0.5(3)	0.26
P			
$x$	0.2867(5)	0.288(4)	0.2879(1)
$y$	0	0	0
$z$	1/4	1/4	1/4
$B(\text{\AA})^2$	0.72(8)	1.7(4)	0.28
O <sub>1</sub>			
$x$	0.1786(4)	0.182(2)	0.1802(2)
$y$	0.98278(4)	0.985(2)	0.9848(2)
$z$	0.1888(1)	0.1894(6)	0.1883(1)
$B(\text{\AA})^2$	1.60(7)	1.8(5)	0.85
O <sub>2</sub>			
$x$	0.1849(3)	0.186(1)	0.1845(2)
$y$	0.1595(3)	0.160(2)	0.1593(2)
$z$	0.0829(1)	0.0826(6)	0.0821(1)
$B(\text{\AA})^2$	0.93(6)	0.5(2)	0.65
$R_f$ %	5.5	3.8	$R$ % 2.4
$R_w$ %	6.9	4.8	$R_w$ % 2.4

some interatomic angles and distances obtained from Rietveld refinements are given in Table V.

### Structure Description

The structure of  $\text{LiGe}_2(\text{PO}_4)_3$  consists of a three-dimensional framework of  $\text{PO}_4$  tetra-

hedra and  $\text{GeO}_6$  octahedra sharing common corners. As emphasized before, lithium ions occupy only the  $M_1$  site which is a trigonal antiprism elongated along the  $c$ -axis (Fig. 3).

The Ge–O distances of the distorted  $\text{GeO}_6$  octahedra (1.834 and 1.872  $\text{\AA}$ ) are equal to or shorter than the values reported for  $\text{GeO}_6$  of rutile-type structure: 1.872 and 1.902  $\text{\AA}$  (11).

The  $\text{PO}_4$  tetrahedra are rather regular with a weak angular dispersion of the O–P–O angles between 104.2 and 113.8° around the ideal value of 109.45°. The P–O<sub>1</sub> and P–O<sub>2</sub> distances have an average value of 1.525  $\text{\AA}$ , which is close to the P–O distances found for  $\text{LiTi}_2(\text{PO}_4)_3$  (1.530  $\text{\AA}$ ) (9),  $\text{LiZr}_2(\text{PO}_4)_3$  (1.522  $\text{\AA}$ ) (10), or  $\text{NaZr}_2(\text{PO}_4)_3$  (1.543  $\text{\AA}$ ) (7).

Assuming the lithium atoms to be located at the center of the  $M_1$  site, the Li–O distance (2.210  $\text{\AA}$ ) is very close to that expected from Shannon's table (2.16  $\text{\AA}$ ) (17) but significantly lower than those found for  $\text{LiTi}_2(\text{PO}_4)_3$  [2.26  $\text{\AA}$  (9)] and even more so for  $\text{LiZr}_2(\text{PO}_4)_3$  [2.491  $\text{\AA}$  (10)]. All these values are consistent with the increasing  $c$ -parameter: 20.88  $\text{\AA}$  (Ti) and 22.24  $\text{\AA}$  (Zr).

### Thermal Structure Evolution of $\text{LiGe}_2(\text{PO}_4)_3$

Between 300 and 1000 K the Ge–O distances remain remarkably constant but both P–O<sub>1</sub> and P–O<sub>2</sub> distances reach progressively the same value (1.5075  $\text{\AA}$ ) at 900 K

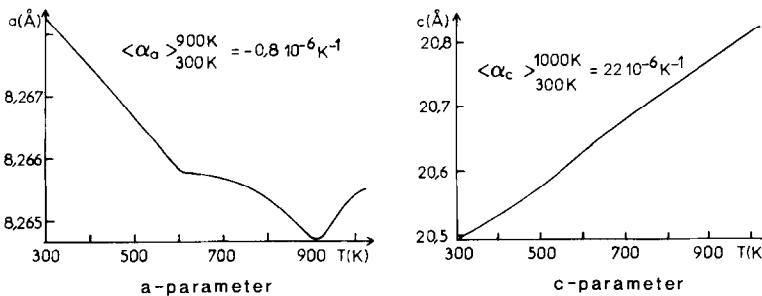


FIG. 2. Thermal expansion of the  $a$ - and  $c$ -parameters of  $\text{LiGe}_2(\text{PO}_4)_3$  between 300 and 1000 K.

TABLE V  
THERMAL EVOLUTION OF  $\text{LiGe}_2(\text{PO}_4)_3$ : Interatomic Angles and Distances

	300 K	400 K	600 K	800 K	900 K	1000 K
<b>Distances(<i>R</i>)</b>						
P-O <sub>1</sub>	1.498(1)	1.496(3)	1.502(7)	1.504(2)	1.506(3)	1.517(2)
P-O <sub>2</sub>	1.527(5)	1.527(1)	1.516(1)	1.512(8)	1.507(8)	1.5175
⟨P-O⟩	1.5125	1.5117	1.5094	1.5085	1.5071	1.5173
Ge-O <sub>1</sub>	1.849(7)	1.847(9)	1.849(2)	1.848(6)	1.847(2)	1.839(1)
Ge-O <sub>2</sub>	1.865(2)	1.870(1)	1.862(7)	1.865(6)	1.870(1)	1.855(6)
⟨Ge-O⟩	1.8575	1.859	1.856	1.857	1.858	1.847
⟨Li-O⟩	2.210	2.234	2.257	2.274	2.288	2.285
<b>Angles(°)</b>						
O <sub>1</sub> -P-O <sub>1</sub>	113.50	113.9	110.13	108.94	108.37	107.18
O <sub>2</sub> -P-O <sub>2</sub>	109.44	109.65	112.83	114.13	114.12	114.44
O <sub>1</sub> -P-O <sub>2</sub>	104.34	104.27	104.84	105.09	104.90	105.02
O <sub>1</sub> -P-O <sub>2</sub>	112.69	112.65	112.16	112.00	112.27	112.36

and then increase. The mean ⟨Li-O⟩ distance increases also between 300 and 900 K and then remains constant. A similar evolution had been observed for  $\text{NaZr}_2(\text{PO}_4)_3$  (19).

The flexibility of the  $M(\text{IV})_2(\text{PO})_3$  skeleton allows a rotation of the oxygen atoms around the *c*-axis at the  $M_1$  site, alternatively clockwise and counterclockwise, involving a rotation of the  $\text{PO}_4$  groups schematized in Fig. 4.

All these displacements result in an elongation of the  $M_1$  antiprism along the *c*-axis.

A mechanism for such thermal behavior was postulated by Lenain *et al.* (13). The

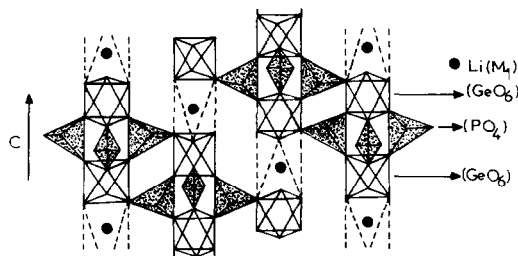


FIG. 3. Schematic drawing of the skeleton of the  $\text{LiGe}_2(\text{PO}_4)_3$ .

shifts of both polyhedra can be described by a projection of the  $[\text{MO}_6]$  octahedron onto the plane perpendicular to the *c*-axis and a

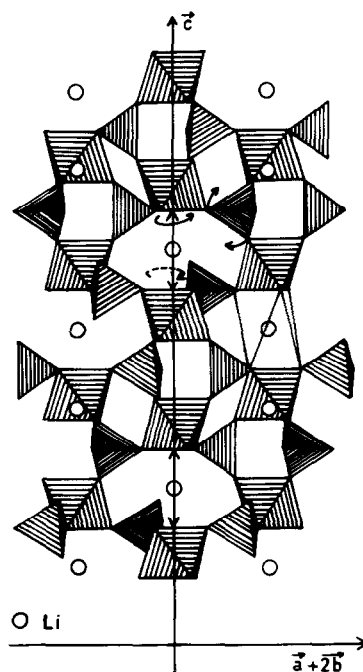


FIG. 4. Mechanism of the thermal expansion of  $\text{LiGe}_2(\text{PO}_4)_3$ .

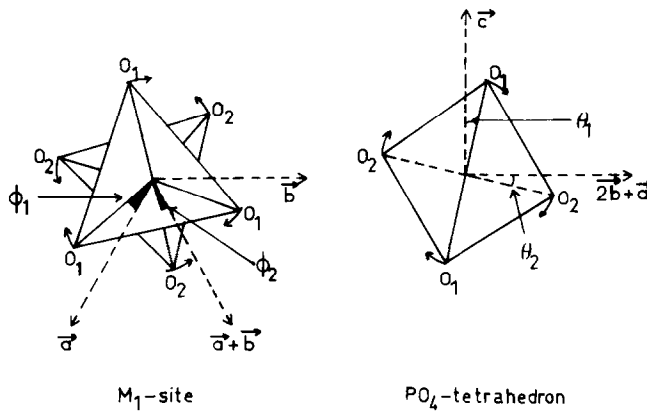


FIG. 5. Oxygen displacement around the  $M_1$  site and for the  $\text{PO}_4$  tetrahedron (according to Lenain *et al.* (13)).

projection of the  $\text{PO}_4$  tetrahedron onto the plane perpendicular to the  $a$ -axis. The movements of oxygen are characterized by the  $\phi_1$  and  $\theta_1$  angles for  $\text{O}_1$ , and  $\phi_2$  and  $\theta_2$  for  $\text{O}_2$ , which are defined in Fig. 5.

The results collected in Table VI show clearly that  $\text{O}_1$  shifts more than  $\text{O}_2$  in agreement with the previous variations reported in  $\text{NaTi}_2(\text{PO}_4)_3$  (15) and  $\text{NaZr}_2(\text{PO}_4)_3$  (19).

Owing to the similarity of the mechanism shown for thermal expansion in such materials, it was worthwhile to relate the thermal expansion coefficients to the structural parameters of the phases at room temperature in order to show that the thermal behavior

could be predicted from the structural information.

#### Conclusion: The Thermal Expansion of Nasicon-Type Phosphates $M(\text{I})M(\text{IV})_2(\text{PO}_4)_3$

The relations between the crystal structure of  $\text{NaZr}_2(\text{PO}_4)_3$ -type compounds and the thermal expansion have been investigated previously by several authors (12–16, 19, 21). In the present discussion are mentioned only the results concerning phosphates with composition  $M(\text{I})M(\text{IV})_2(\text{PO}_4)_3$ , where the monovalent ions are lo-

TABLE VI  
APPLICATION OF LENAIN'S MODEL (13) TO THE THERMAL EXPANSION OF  $\text{LiGe}_2(\text{PO}_4)_3$ : THERMAL EVOLUTION OF THE INTERNAL PARAMETERS

	300 K	400 K	600 K	800 K	900 K	1000 K
$\theta_1^\circ$	5.01	5.22	5.80	6.34	6.70	7.00
$\theta_2^\circ$	0.94	0.60	0.70	1.30	1.56	2.02
$\theta_1 - \theta_2^\circ$	4.07	4.62	5.11	5.04	5.14	4.98
$\phi_1^\circ$	4.11	4.24	4.60	5.00	5.29	5.61
$\phi_2^\circ$	7.53	7.70	8.28	8.86	8.55	8.26
$\phi_2 - \phi_1^\circ$	3.42	3.46	3.68	3.66	3.26	2.65

TABLE VII  
CELL PARAMETERS AND AVERAGE INTERATOMIC DISTANCES OF  
VARIOUS NASICON-TYPE PHOSPHATES:  $M(\text{I}) [M(\text{IV})]_2(\text{PO}_4)_3$

	$\langle \text{P-O} \rangle$ (Å)	$\langle M(\text{IV})-\text{O} \rangle$ (Å)	$\langle M(\text{I})-\text{O} \rangle$ (Å)
$\text{LiTi}_2(\text{PO}_4)_3$ (9) $a = 8.52$ Å $c = 20.88$ Å	1.530	1.930	2.260
$\text{NaTi}_2(\text{PO}_4)_3$ (15) $a = 8.4876$ Å $c = 21.801$ Å	1.510	1.948	2.472
$\text{LiZr}_2(\text{PO}_4)_3$ (10) $a = 8.847$ Å $c = 22.243$ Å	1.522	2.061	2.499
$\text{NaZr}_2(\text{PO}_4)_3$ (7) $a = 8.8043$ Å $c = 22.7585$ Å	1.531	2.066	2.538
$\text{KZr}_2(\text{PO}_4)_3$ (18) $a = 8.71$ Å $c = 23.89$ Å	1.522	2.063	2.813

cated in the  $M_1$  site. The cell parameters are obtained and mean interatomic distances are summarized in Table VII for phosphates whose detailed structural determinations have been published.

The thermal expansion coefficients are given in Tables VIII and IX as far as they are known.

The  $\langle \text{P-O} \rangle$  and  $\langle M(\text{IV})-\text{O} \rangle$  distances are quite constant [they are close to the values given in Shannon's table (17)]. The  $c$ -parameters are influenced by the size of the  $M(\text{I})$  cations and the thermal expansion along the  $c$ -axis  $\alpha_c$  is connected to the stretching of the  $\text{MO}_6$  antiprism: a wide  $M(\text{I})$  size brings about a larger stretching expansion already at room temperature and a lower  $\alpha_c$ . Such a trend was qualitatively observed in (16, 19) for the  $MZr_2(\text{PO}_4)_3$  ( $M = \text{Li, Na, K}$ ) phosphates.

At room temperature, for a given  $M(\text{IV})$  element  $a$  decreases as the ionic radius of  $M(\text{I})$  increases. In correlation, the thermal expansion of the  $M_1$  site gives rise to contraction of the cell in a direction perpendicular to the  $c$ -axis and the expansion coefficient along the  $a$ -axis becomes negative. This shrinkage is limited by the distortion

possibility of the strongly covalent  $\text{PO}_4$  groups and their ability to move. Obviously a limitation of such an evolution will be quickly attained for compounds with a relatively low  $a$ -parameter such as  $\text{LiGe}_2(\text{PO}_4)_3$ .

A very simple model can account for the  $\alpha_a$  and  $\alpha_c$  values found for  $\text{LiGe}_2(\text{PO}_4)_3$ . Since the  $\langle M(\text{IV})-\text{O} \rangle$  distances are practically temperature independent the tensions along the  $c$ -axis can be characterized by the  $\langle M(\text{IV})-\text{O} \rangle$  distance over the  $c$ -parameter ratio (labeled as  $\delta$ ) and along the  $a$ -axis by the  $\langle M(\text{IV})-\text{O} \rangle$  distance over the  $a$ -parameter

TABLE VIII  
 $\langle \alpha_c \rangle$  ( $\text{K}^{-1}$ ) AND  $\delta$  PARAMETERS OF VARIOUS  
NASICON-TYPE PHOSPHATES  $M(\text{I})[M(\text{IV})]_2(\text{PO}_4)_3$  (SEE  
TEXT)

Phosphates	$10^6 \alpha_c$ ( $\text{K}^{-1}$ )	$10^2$
$\text{LiZr}_2(\text{PO}_4)_3$ (16)	24	9.27
$\text{LiZr}_2(\text{PO}_4)_3$ (21)	28.9	9.32
$\text{NaZr}_2(\text{PO}_4)_3$ (16)	23	9.08
$\text{LiZr}_2(\text{PO}_4)_3$ (19)	22.4	
$\text{LiGe}_2(\text{PO}_4)_3$	22	9.05
$\text{NaTi}_2(\text{PO}_4)_3$ (15)	21.3	8.93
$\text{KZr}_2(\text{PO}_4)_3$ (13, 16)	0	8.63



TABLE IX  
 $\langle\alpha_a\rangle$  ( $\text{K}^{-1}$ ) AND  $\gamma$  PARAMETERS OF VARIOUS NASICON-TYPE PHOSPHATES  $M(\text{I})[M(\text{IV})_2(\text{PO}_4)_3]$  (SEE TEXT)

Phosphates	$10^6 \langle\alpha_a\rangle$ ( $\text{K}^{-1}$ )	$\gamma$
$\text{LiZr}_2(\text{PO}_4)_3$ (16)	-10	0.2330
$\text{LiZr}_2(\text{PO}_4)_3$ (21)	-5.53	0.2329
$\text{NaZr}_2(\text{PO}_4)_3$ (16)	-6.4	0.2346
$\text{LiZr}_2(\text{PO}_4)_3$ (19)	-5.4	
$\text{KZr}_2(\text{PO}_4)_3$ (16, 13)	-5	0.2368
$\text{NaTi}_2(\text{PO}_4)_3$ (15)	-4.45	0.2295
$\text{LiGe}_2(\text{PO}_4)_3$	-0.8	0.2240

ter ratio (i.e.,  $\gamma$ ). As the strains increase,  $\alpha_c$  and  $\delta$  increase and  $\gamma$  and  $\alpha_a$  decrease. Table VIII and IX list the  $\delta$  and  $\gamma$  values by considering only the  $\langle M(\text{IV})\text{-O}\rangle$  distances deduced from a detailed RT structure determination.

For a given  $M(\text{IV})$  (e.g., zirconium), a larger  $M(\text{I})$  size leads to a lower  $a$ -parameter, which becomes obviously less shrinkable. As a result  $|\langle\alpha_a\rangle|$  becomes smaller. For a given  $M(\text{I})$  cation, as the size of  $M(\text{IV})$  decreases [e.g.,  $\text{NaTi}_2(\text{PO}_4)_3$  with respect to  $\text{NaZr}_2(\text{PO}_4)_3$  or  $\text{LiGe}_2(\text{PO}_4)_3$  compared to  $\text{LiZr}_2(\text{PO}_4)_3$ ]  $a$  decreases as well as  $|\langle\alpha_a\rangle|$ .

The behavior of  $\text{LiGe}_2(\text{PO}_4)_3$  can be understood as an extrapolation of both trends, leading to a small negative value of  $\alpha_a$ , which becomes positive only at about 900 K.

Finally it is worthwhile to plot  $\gamma$  against  $f(M(\text{IV})\text{-O})$  for the lithium and sodium phosphates (Fig. 6).

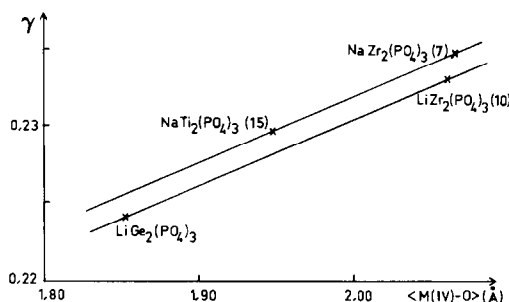


FIG. 6. Variation of  $\gamma$  versus  $\langle M(\text{IV})\text{-O}\rangle$  distances for various Nasicon-type phosphates (see text).

The two graphs are parallel, which confirms the similarity of the mechanism of internal adjustment observed for the structure.

Indeed such a comparison is only valid when the cationic distribution within the materials is not influenced by the elaboration process (21).

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